Practice Problems

1. Find
$$\lim_{x \to 4} \frac{x^2 - 25}{x^2 - 16}$$

Numerator approaches 16 - 25 = -9. Denominator gets close to 0, but +0 if we go from numbers greater than 4 and -0 if we take numbers less than 4. So, there is no limit.

2. Find
$$\lim_{x \to \infty} \frac{x^2 - 25}{x^2 - 16}$$

Divide all terms by x^2 . The limit is 1.

3. Find
$$\lim_{x \to 0} \frac{x^2 - 25}{x^2 - 16}$$

There is no problem with dividing by 0, so just plug in. -25/-16 = 1.5625

Answer each question using the given information.

4.
$$\lim_{x \to 4+} f(x) = 7$$
 and

$$\lim_{x \to 4^-} f(x) = 5$$

So,
$$\lim_{x \to 4} f(x) =$$

b) 5

d) Cannot be determined from this information.

5.
$$\lim_{X \to 0+} f(x) = 12$$

and
$$\lim_{x \to 0^{-}} f(x) = 12$$

$$\lim_{x \to 0^{-}} f(x) = 12 \qquad \text{So, } \lim_{x \to 0} f(x) = 0$$

c) Does not exist.

d) Cannot be determined from this information.

6.
$$\lim_{x \to -2+} f(x) = 3$$
 and

$$\lim_{x \to -2^{-}} f(x) = 3$$
 $f(-2) = 10$

$$f(-2) = 10$$

So,
$$\lim_{x\to 0} f(x) =$$

b) 10

c) Does not exist. d) Cannot be determined from this information.

7.
$$\lim_{x \to -7+} f(x) = 10$$

7.
$$\lim_{x \to -7+} f(x) = 10$$
 and $\lim_{x \to -7-} f(x) = 10$

$$\lim_{x \to -7} f(x) = 10.$$
 So, $f(-7) =$

b) -7

c) Does not exist. (d) Cannot be determined from this information